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BLOCKING THE $\beta^{\prime} s$ in the ${ }^{16} \mathrm{~N}$ SOURCE
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## 1 Introduction

The decision will have to be made as to whether or not it is desirable to block out the $\beta$ 's from the ${ }^{16} \mathrm{~N}$ source, but first it must be determined to what extent the Cerenkov radiation from the $\beta$ decays can be attenuated. The $\mathrm{D}_{2} \mathrm{O}$ option is used for the calculations, assuming 1 inch ID acrylic pipe with a $1 / 4$ inch thick wall. The detector response is calculated for both a clear and blackened acrylic tube. The bottom line is that a blackened tube very effectively blocks out the $4.27 \mathrm{MeV} \beta$ and there is very little distortion of the $6.13 \mathrm{MeV} \gamma$ from the $10.4 \mathrm{MeV} \beta$. There are many figures and one table in this report so for those of you who just want the final result, I refer you to the final figure which shows.
a) Detector response to a 'pure' $6.13 \mathrm{MeV} \gamma$.
b) Detector response to ${ }^{16} \mathrm{~N}$ with a blackened acrylic tube
c) Detector response to ${ }^{16} \mathrm{~N}$ with a clear acrylic tube

## 2 Results Assuming a Black Pipe

A simple EGS4 program is used for the calculation instead of using the full blown detector MC. The number of Cerenkov photons is calculated at each step EGS4 takes, then scaled down to the the number of PMT's predicted by the Queens MC, which is then given a Poissonian variation. The regions 1) smaller than the inner radius of the acrylic tube 2) between the acrylic radii and 3) outside the acrylic are taken to be $\mathrm{D}_{2} \mathrm{O}$, acrylic and $\mathrm{H}_{2} \mathrm{O}$ respectively. 100 K events are generated uniformly in the $\mathrm{D}_{2} \mathrm{O}$ for the $6.13 \mathrm{MeV} \gamma$ and each of the $\beta$ 's. Table I shows the number of events generating Cerenkov light in each of the three regions for each of the three radiations. The last line in the table shows the number of events that have an electron in the $\mathrm{H}_{2} \mathrm{O}$ region.

So while the $4.27 \mathrm{MeV} \beta$ has 3311 electrons leaking out of the acrylic, only 1325 will generate Cerenkov radiation, out of the 100 k generated.

## $2.1 \quad$ 6.13 MeV $\gamma$ Outside Pipe

Fig 1 overlays the PMT response to a 'pure' $6.13 \mathrm{MeV} \gamma$ with those that escape the acrylic pipe. While some events occur at low NPMT, the overall 6.13 MeV shape remains virtually undistorted.

### 2.2 4.24 MeV $\beta$ Outside Pipe

In Fig 2 the $98431,6.13 \mathrm{MeV} \gamma$ events are compared with the $1325,4.27 \mathrm{MeV} \beta$ events that make Cerenkov light outside the acrylic. The combination of the low fraction of $4.27 \mathrm{MeV} \beta$ that escape ( $3.3 \%$ ) and the small amount of Cerenkov light they generate results in no distortion of the $6.13 \mathrm{MeV} \gamma$ spectrum as shown in Fig 3 where the convolution of the two is compared with the $6.13 \mathrm{MeV} \mathrm{\gamma}$ alone.

### 2.3 10.4 MeV $\beta$ Outside Pipe

Fig 4 shows the detector response from the Cerenkov radiation generated in each of the three regions individually as well as the sum. The relative amplitude of the 10.4 $\mathrm{MeV} \beta$ is 0.38 that of of the $6.13 \mathrm{MeV} \gamma$. Fig 5 overlays the $10.4 \mathrm{MeV} \beta$ spectrum, weighted by 0.38 with that of the $6.13 \mathrm{MeV} \gamma$ outside the acrylic. The simple sum of these two (as opposed to the convolution required for the $4.27 \mathrm{MeV} \beta$ ) is shown in Fig 6 in overlay with an undistorted $6.13 \mathrm{MeV} \gamma$. There is some distortion of the 6.13 MeV spectral shape below the lower half point but above that there is no discernible distortion and the peak position remains unaffected.

## 3 Results with a Clear Pipe

The detector response of the $4.27 \mathrm{MeV} \beta$ from all three regions now has to be convolved with the 6.13 MeV . The $\gamma$ and $4.27 \mathrm{MeV} \beta$ are shown in Fig 7 along with their convolution. This is now added to the $10.4 \mathrm{MeV} \beta$ spectrum weighted by 0.38 . (Fig 8)

## 4 Conclusion

The comparison of 'pure' $6.13 \mathrm{MeV} \gamma$ with that of a clear pipe and a blackened pipe is shown in Fig 9. The blackened pipe leaves the 6.13 MeV spectral shape virtually undistorted above the low $1 / 2$ point, with the $4.27 \mathrm{MeV} \beta$ all but totally eliminated.. The $10.4 \mathrm{MeV} \beta$ causes some distortion below the lower $1 / 2$ point, but any correction is of second order compared to the spectral response with a clear pipe.

Thus the option exists for eliminating the $\beta$ 's from the ${ }^{16} \mathrm{~N}$ source to the extent that there is virtually no distortion of the 6.13 MeV energy spectrum above 40 PMT and only a second order distortion above 30 PMT.

TABLE I
Number of Events Generating Cerenkov Light
100k Events Generated

| Region | Number of Events |  |  |
| :---: | :---: | :---: | :---: |
|  | $4.27 \beta$ | $10.4 \beta$ | $6.13 \gamma$ |
| $\mathrm{D}_{2} \mathrm{O}$ | 91812 | 95918 | 4046 |
| Acrylic | 21622 | 60531 | 5470 |
| $\mathrm{H}_{2} \mathrm{O}$ | 1325 | 32859 | 98431 |


| Number of Events with Electrons |  |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{H}_{2} \mathrm{O}$ | 3311 | 38518 | 99809 |



Pure 6.13 MeV $\gamma$ - One inch pipe


Fig 1

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Pure 6.13 MeV $\gamma$ and $4.27 \mathrm{MeV} \beta$ Spectrum Outside Pipe


Fig 2

Convolution of $6.13 \mathrm{MeV} \gamma$ and $4.27 \mathrm{MeV} \beta 1$ inch pipe


Fig. 3


Fig. 4
$6.13 \mathrm{MeV} \gamma$ and $0.38 \times 10.4 \mathrm{MeV} \beta$ Outside Acrylic Wall


Fig. 5


Fig. 6


Fig. 7

Convolution, 10.4 $\mathrm{MeV} \beta$ and Sum


Fig. $\mathcal{E}$


Fig. 9

