# The Shape of the Acrylic Vessel 

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## 1 Summary

This report presents the results of the surveys of the acrylic vessel. The results for the upper half are only summarized here, as the details were previously reported in SNO-STR-97-053. The results for the lower half of the vessel are reported in detail here. As a whole, the vessel was found to be spherical within the design tolerance of $\pm 0.5^{\prime \prime}$, with an inner radius of $236.38^{\prime \prime}$.

## 2 The Upper Half of the Vessel

The results of the survey of the upper half of the acrylic vessel are presented in detail in the SNO internal report SNO-STR-97-053 ("The Shape of the Upper Half of the Acrylic Vessel Prior to Hanging it on Ropes"). As such, only a summary of the results are presented here, and the reader is referred to the above document for more details.

### 2.1 Description of the Surveying

After the upper half of the acrylic vessel was completed, but prior to its being lifted off the platform and suspended freely on the ropes, targets were placed on the inside surface of all of the panels, and the dome was surveyed. There were generally three targets placed on each panel (at the lower left, middle and upper right areas), with two extra targets placed on the rope groove panels (at the upper left and lower right areas). In addition to these, a target was also placed on the bottom edge of every 102 panel. A total of 231 targets were used to survey the shape of the dome.

The surveying was done in two parts: the 101-106 panels were shot on Nov 28, and the 108-110 and 102 bottoms were shot on Dec 16. A common reference frame was used when comparing and combining the two datasets. The reference frame had its origin at the center of the construction platform, and defined the nominal axis of symmetry of the vessel and PSUP. As a consistency check, the best-fit sphere to each dataset was calculated separately, and compared. The centers differed by $0.048^{\prime \prime}$, and the spherical radii by $0.015^{\prime \prime}$, showing that the results were consistent. The two datasets were then combined, and fit as a whole.

### 2.2 Results of the Surveys

The results of the spherical fit to the whole upper half of the acrylic vessel are shown below:

$$
\begin{gathered}
\text { vessel center }(\mathrm{x}, \mathrm{y}, \mathrm{z})=(0.042,0.020,91.550) \\
\text { radius }=236.383 \\
\text { maximum deviations }=+0.200,-0.233
\end{gathered}
$$

The nominal values are:

$$
\begin{gathered}
\text { vessel center }(\mathrm{x}, \mathrm{y}, \mathrm{z})=(0.0,0.0,91.591) \\
\text { radius }=236.43
\end{gathered}
$$

Hence, the best-fit sphere center was found to deviate from the nominal value by $0.06^{\prime \prime}$, and the spherical radius deviated from the nominal value by $-0.05^{\prime \prime}$. As the acrylic panels in the upper half of the vessel are slightly thicker than the nominal thickness of $2.17^{\prime \prime}$, the reduced spherical radius is not undesirable. The variation in the spherical radius of $\pm 0.23^{\prime \prime}$ was well within the design tolerance of $\pm 0.5^{\prime \prime}$.

The bottom edge of the upper half of the vessel showed a slight elliptical distortion. The spherical radius varied by $\pm 0.17^{\prime \prime}$, and the height by $\pm 0.023^{\prime \prime}$. The major axis of the ellipse was approximately aligned in the East-West direction, and the minor axis in the North-South direction.

## 3 The Lower Half of the Vessel

The results of the surveys of the lower half of the acrylic vessel are presented here in detail. Unlike the upper half, the lower half of the vessel could not be surveyed in its entirety upon completion. Instead, we have had to rely on the results of partial surveys done after each row of panels was completed. Some details of the construction and surveying work on the lower half are given here as they are relevant for estimating the accuracy of the presented results.

### 3.1 Construction

After the upper half of the vessel was lifted and hung freely on the ropes, the bottom of the equator was surveyed and the ropes adjusted until the vessel was level to within $\pm 0.020^{\prime \prime}$. The vessel was built downwards row-by-row, with the panels in each row being aligned, bonded to each other into a ring, and then bonded to the rest of the vessel at each stage. Before setting and aligning each row of panels, the platform was lowered about $10^{\prime}$ below the bottom edge of the vessel and supported on scaffolding. The panels were supported on a steel jig on the platform during the aligning and bonding processes. The presence of the jig and the upward curvature of the lower part of the vessel made it difficult to access (and thus clean) the inside of the acrylic above the bottom two rows of panels. Hence, it was decided that a final cleaning of the row next to the bottom would be done prior to lowering the platform at the end of each stage, and that the cleaned panels would be protected by a tarp during the construction of the rest of the vessel below.

For quality bonds, the gaps between the panels into which the bonding syrup was poured had to be a width of $0.125^{\prime \prime} \pm 0.063^{\prime \prime}$. This, in effect, constrained the panels to be positioned within $\sim 0.15^{\prime \prime}$ of the nominal spherical radius and to within $\sim 0.10^{\prime \prime}$ of the nominal height.

The variation in height and radius between adjacent panels was usually much less than this $\left(\leq 0.08^{\prime \prime}\right)$, to ensure that the panels overlapped well. Thus, the bonding process forced the alignment of the panels to be well within the $\pm 0.5^{\prime \prime}$ tolerance specified by considerations of the overall vessel strength.

The final shape of the vessel is determined, not only by the original alignment of the panels prior to bonding, but also by deformation caused by mild internal stresses set up during the bonding process. Such a deformation was noticed when the upper half of the vessel was lifted off the supporting jig and hung freely on the ropes. The elliptical deformation of the equator had increased such that the spherical radius varied by $\pm 0.54^{\prime \prime}$, and the height by $\pm 0.09^{\prime \prime}$. The major axis of the ellipse was still in the East-West direction. As it was impossible to keep the bond gaps and overlaps between panels on the lower half within the tolerances with such a large distortion, the vessel was brought back into round during the aligning and bonding processes. This was accomplished during alignment with two sets of ropes and suction cups along the major axis of the vessel, each pulling with a force of less than 300 lbs (the force required to pop the suction cup free). During bonding, the extension arms on the jig that held the panels were used to make the vessel rounder.

### 3.2 Surveying

The method of construction of the lower half of the vessel introduced the following constraints for the surveying:
i) because of the problem of accessibility, surveying targets were only placed on the two bottom rows of panels, and the ones on the higher of the two rows were removed when the panels were cleaned prior to lowering the platform. To make cleaning easier, only one target was placed on the face of each accessible panel (although many were placed temporarily on the dirty bottom edge of the vessel during surveying, as described below). This meant that a complete survey of the bottom half of the vessel could not be done as for the upper half (there would also be a problem with setting up the theodolites within the vessel for such a job).
ii) when the ropes or extension arms that were used to make the vessel rounder were removed, the elliptical distortion would return to some lesser degree (as shown below). The final survey of each row was done with the ropes and extension arms removed, so the elliptical distortion is visible in the results. However, as the bonding of subsequent rows probably further reduced the distortion of the vessel, the results of the final survey for each row can't be said to represent the positions of those panels on vessel completion. Rather, it is more likely that the survey results provide upper estimates of the deviation of the final radius from the nominal value at each target location.
iii) when the platform was lowered at the end of each stage, its new absolute position was only known to an accuracy of a few inches. Thus, the center of the platform could no longer be used to define the nominal center of the vessel as it was for the upper half. Instead, the nominal sphere center had to be defined at each stage using the accessible portion of the vessel, itself. This was done by surveying the bottom edge of the vessel, fitting those points with a circle, and translating upward from the circle center the nominal distance to the sphere center. As a check, an alternate method was used to estimate the sphere center in two of the jobs. The coordinates of the 103 targets were determined in the sphere center

Table 1: Average Spherical Radius and Maximum Deviations

| Row | Avg. Rad. <br> (in) | Max. Pos. Dev. <br> (in) | Max. Neg. Dev <br> (in) |
| :---: | :---: | :---: | :---: |
| 101 | 235.063 | 0.361 | -0.432 |
| 103 | 236.367 | 0.265 | -0.292 |
| 105 | 236.310 | 0.188 | -0.216 |
| 107 | 236.318 | 0.169 | -0.144 |
| $103-107$ | 236.331 | 0.301 | -0.256 |

frame of the $101 / 103$ survey job (Mar 23, 1997). The coordinate frame that best reproduced these old target coordinates in the new $103 / 105$ job was used to estimate the position of the sphere center in the latter job. The two sphere centers got with the different methods differed by only $0.063^{\prime \prime}$. Likewise, using the old coordinates of the 105 targets to estimate the alternate sphere center in the $105 / 107$ job produced a difference of $0.056^{\prime \prime}$ between the two sphere centers. Thus, the method used to estimate the sphere center is accurate enough for the present measurements.
iv) the 107 row was the last to be surveyed using the theodolites. Once the 109 panels were in position, there wasn't enough room to set up the theodolites in the hole in the vessel left for the bottom plug. Instead, the bond gaps, overlaps and circularity of the hole for the bottom plug were used to determine when the panels were in position. As a final check, the distance from the top of the chimney to the vessel bottom was measured and compared to the nominal distance to deduce the spherical radius at which the plug was set.

### 3.3 Surveying Results for the 101, 103, 105 and 107 Rows

Figure 1 shows the spherical radius of the 101 panels after the 103 panels were bonded beneath them. The spherical radius of the target near the middle of each panel in the 103 and the 105 rows is also shown in Figures 2 and 3, respectively. In the latter two cases, the results before and after the subsequent row was added are shown, indicating how the vessel improved its shape between each set of readings. Figure 4 only shows the spherical radius of the 107 row before the 109 panels were added, since there are no survey results following that job.

Table 1 shows the average spherical radius and the maximum deviations based on the last survey for each row, as well as the results for the combined 103-107 rows. The average radius for the 101 panels is smaller than for the other panels because the targets were placed on the thick portions of the rope groove panels. The numbers indicate that the deviations from sphericity decreased with each new row. What is not known is whether the deviations for the higher rows decreased later as the lower rows were added. The before and after data for the 103 and 105 rows indicate that this is likely, but to an unknown degree. So, it seems best to treat the last surveyed positions as maximum deviations from sphericity rather than the final coordinates for the panels.

For reference, the target coordinates given in the sphere center frame for all three survey jobs are tabulated in the Appendices to this report.


Figure 1: Spherical Radius of the 101 Panels.


Figure 2: Spherical Radius of the 103 Panels.


Figure 3: Spherical Radius of the 105 Panels.


Figure 4: Spherical Radius of the 107 Panels.

### 3.4 Spherical Radius of the Bottom Plug

On Jan 12, 1998, the distance from the top of the chimney to the bottom of the vessel was measured with a steel tape to be $742.59^{\prime \prime} \pm 0.05^{\prime \prime}$. The nominal distance can be calculated based on previous measurements of the distance from the top of the chimney to the center of the vessel. On Mar 23, 1997, when the $101 / 103$ final survey was shot, a steel tape was lowered from the top of the chimney into the vessel. A point on the steel tape inside the vessel was shot using the calibrated surveying system, thus determining its height relative to the bottom of the 103 panels as $26.253^{\prime \prime}$. That point on the tape was $574.173^{\prime \prime}$ below the top of the chimney. Given that the nominal distance from the bottom of the 103 panels to the center of the vessel is $94.3^{\prime \prime}$, that put the center of the vessel a distance of $506.126^{\prime \prime}$ below the top of the chimney. A pair of similar measurements relative to the bottom of the 107 panels (taken on Aug 8 and Aug 17, 1997) yielded distances of $506.285^{\prime \prime}$ and $506.059^{\prime \prime}$, respectively. Based on these three sets of measurements, the center of the vessel is estimated to be $506.16^{\prime \prime} \pm 0.12^{\prime \prime}$ below the top of the chimney. Adding the nominal inside radius of the vessel $\left(236.43^{\prime \prime}\right)$ to the distance from the top of the chimney to the center of the vessel yields an expected distance of $742.59^{\prime \prime} \pm 0.12^{\prime \prime}$ from the top of the chimney to the bottom of the vessel. That is exactly equal to the result measured on Jan 12, 1998, indicating that the 109 panels and bottom plug are in the correct position relative to the rest of the bottom of the vessel.

## 4 Conclusions

Prior to hanging it on ropes, the upper half of the acrylic vessel was seen to be spherical, with a radius of $236.38 \pm 0.23^{\prime \prime}$. When hung freely on the ropes, an elliptical distortion of $\pm 0.54^{\prime \prime}$ in the spherical radius became apparent in the equatorial region of the vessel. As it was impossible to keep the bond gaps and overlaps between panels on the lower half within the tolerances with such a large distortion, the vessel was brought back into round during the aligning and bonding processes. When allowed to hang free after each new row was added, the distortion would reappear, but to a lesser extent each time. Since the higher rows could not be re-surveyed after the lower rows were added, the final shape of the vessel is not precisely known. However, the results of the last survey for each row probably provide upper extimates of the deviation from sphericity. Combining the results for the lower half of the vessel (including the 109 panels and the bottom plug), the average spherical radius was seen to be close to the value of $236.38^{\prime \prime}$ obtained for the upper half of the vessel. The deviations from sphericity in the lower half were at most $\pm 0.30^{\prime \prime}$, and were likely to be less at the completion of the vessel. For the upper half of the vessel, only the 101 panels were surveyed after the 103 row was bonded on. At that time, the largest deviation from sphericity was $0.43^{\prime \prime}$. It is likely that the deviations are smaller with the completion of the lower half of the vessel, and will certainly be less than the design tolerance of $\pm 0.5^{\prime \prime}$.

## 5 Appendix A

## Measure

EVENT SUMMARY

Job Name: 970323-2 101/103 ROW
Date: 98/02/15
Operator: robk
Job Comments:
Survey of the 101/103 panels taken on Mar 23, 1997.
The sphere center was got by fitting a circle to the bottom of the 103 panels, and translating upwards the nominal distance from the circle center.

JOB SUMMARY

VALUES SHOWN IN: R Hand Inch Grads

| Event CS | - | COORDINATES | -------\| | POINTING | APEX | \|----EVENT |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. No. | X | Y | Z | ERROR | ANGLE | NAME |
| Polar | 234.9279 | 86.3514 | 106.0827 |  |  |  |
| 223 | 228.5025 | -49.7535 | -22.4125 | 0.0025 | 0.00 | 101-04-LL |
| Polar | 235.1247 | 74.0690 | 106.0820 |  |  |  |
| 23 3 | 214.9034 | -92.7206 | -22.4286 | 0.0011 |  | 101-04-LR |
| Polar | 235.0018 | 80.2698 | 98.7665 |  |  |  |
| 243 | 223.7637 | -71.6583 | 4.5532 | 0.0003 | 0.00 | 101-04-M |
| Polar | 234.8548 | 86.2912 | 94.0001 |  |  |  |
| 253 | 228.4125 | -49.9602 | 22.1013 | 0.0012 | 0.00 | 101-04-UL |
| Polar | 235.0859 | 74.1555 | 94.0263 |  |  |  |
| 263 | 215.0285 | -92.4281 | 22.0269 | 0.0015 |  | 101-04-UR |
| Polar | 235.3161 | 46.1608 | 105.8860 |  |  |  |
| 273 | 155.3963 | -175.3673 | -21.7256 | 0.0006 |  | 101-02-LL |
| Polar | 235.3491 | 34.1107 | 106.1523 |  |  |  |
| 283 | 119.5938 | -201.4220 | -22.7088 | 0.0004 |  | 101-02-LR |
| Polar | 235.3935 | 40.5695 | 98.8868 |  |  |  |


| 293 | 140.0375 | -189.1631 | 4.1158 | 0.0007 | 101-02-M |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Polar | 235.3627 | 46.3193 | 93.9084 |  |  |
| 303 | 155.8157 | -174.9612 | 22.4868 | 0.0004 | 101-02-UL |
| Polar | 235.3318 | 34.1484 | 93.9965 |  |  |
| 313 | 119.7312 | -201.3814 | 22.1594 | 0.0007 | 101-02-UR |
| Polar | 235.2625 | 6.6787 | 106.3510 |  |  |
| 323 | 24.5133 | -232.8057 | -23.4313 | 0.0007 | 101-05-LL |
| Polar | 235.2426 | -5.7895 | 105.9111 |  |  |
| 33 3 | -21.2719 | -233.2614 | -21.8114 | 0.0009 | 101-05-LR |
| Polar | 235.3688 | 0.1780 | 99.7851 |  |  |
| 343 | 0.6582 | -235.3665 | 0.7947 | 0.0015 | 101-05-M |
| Polar | 235.3126 | 6.2988 | 93.9757 |  |  |
| 353 | 23.1400 | -233.1141 | 22.2342 | 0.0011 | 101-05-UL |
| Polar | 235.2633 | -5.5373 | 93.9353 |  |  |
| 363 | -20.3447 | -233.3112 | 22.3783 | 0.0013 | 101-05-UR |
| Polar | 234.9184 | -33.6647 | 106.0945 |  |  |
| 37 3 | -117.9738 | -201.9026 | -22.4548 | 0.0011 | 101-09-LL |
| Polar | 234.9221 | -45.7502 | 106.1282 |  |  |
| 383 | -153.9482 | -176.0073 | -22.5790 | 0.0014 | 101-09-LR |
| Polar | 235.1837 | -39.4318 | 98.8217 |  |  |
| 393 | -136.5105 | -191.4610 | 4.3526 | 0.0012 | 101-09-M |
| Polar | 235.0560 | -33.6946 | 93.8485 |  |  |
| 403 | -118.1276 | -201.9478 | 22.6777 | 0.0017 | 101-09-UL |
| Polar | 235.0011 | -45.9061 | 94.0087 |  |  |
| 413 | -154.4623 | -175.7249 | 22.0837 | 0.0019 | 101-09-UR |
| Polar | 234.8229 | -73.5349 | 106.1549 |  |  |
| 423 | -213.8195 | -94.3886 | -22.6676 | 0.0019 | 101-08-LL |
| Polar | 234.8164 | -85.7693 | 106.1058 |  |  |
| 43 3 | -227.9218 | -51.8146 | -22.4866 | 0.0019 | 101-08-LR |
| Polar | 235.0178 | -79.7238 | 99.2145 |  |  |


| 443 | -223.1810 | -73.5881 | 2.8997 | 0.0022 |  | 101-08-M |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Polar | 234.9259 | -73.6444 | 93.9625 |  |  |  |
| 453 | -214.1134 | -94.0784 | 22.2463 | 0.0024 |  | 101-08-UL |
| Polar | 234.8347 | -86. 1877 | 93.6633 |  |  |  |
| 463 | -228.1940 | -50.3015 | 23.3361 | 0.0026 |  | 101-08-UR |
| Polar | 234.7310 | -113.8989 | 105.9914 |  |  |  |
| 47 3 | -228.1448 | 50.6162 | -22.0586 | 0.0018 | 0.00 | 101-01-LL |
| Polar | 234.8568 | -125.8931 | 106.0758 |  |  |  |
| 483 | -214.7157 | 92.4879 | -22.3803 | 0.0012 |  | 101-01-LR |
| Polar | 234.8973 | -119.7737 | 98.5884 |  |  |  |
| 493 | -223.6022 | 71.7750 | 5.2081 | 0.0016 |  | 101-01-M |
| Polar | 234.8045 | -113.7996 | 93.9020 |  |  |  |
| 503 | -228.2586 | 50.2679 | 22.4568 | 0.0025 | 0.00 | 101-01-UL |
| Polar | 234.8656 | -125.8837 | 93.9685 |  |  |  |
| 513 | -214.7516 | 92.4658 | 22.2183 | 0.0023 |  | 101-01-UR |
| Polar | 235.0203 | -153.5051 | 106.2169 |  |  |  |
| 523 | -156.0405 | 174.2436 | -22.9146 | 0.0014 |  | 101-03-LL |
| Polar | 235.2359 | -166.1730 | 106.2323 |  |  |  |
| 53 3 | -118.6233 | 201.8311 | -22.9922 | 0.0004 |  | 101-03-LR |
| Polar | 235.0642 | -159.7805 | 98.7759 |  |  |  |
| 543 | -138.7966 | 189.6583 | 4.5197 | 0.0005 |  | 101-03-M |
| Polar | 235.0171 | -153.5500 | 93.7739 |  |  |  |
| 553 | -155.9131 | 174.3488 | 22.9477 | 0.0010 |  | 101-03-UL |
| Polar | 235.1021 | -166.0652 | 93.7855 |  |  |  |
| 563 | -118.9007 | 201.5206 | 22.9136 | 0.0001 | 81.12 | 101-03-UR |
| Polar | 235.2497 | -193.7612 | 105.9312 |  |  |  |
| 57 3 | -22.9175 | 233.1056 | -21.8858 | 0.0008 |  | 101-10-LL |
| Polar | 235.2741 | 194.3347 | 105.9485 |  |  |  |
| 583 | 20.8181 | 233.3208 | -21.9519 | 0.0013 |  | 101-10-LR |
| Polar | 235.4237 | -199.7361 | 98.9655 |  |  |  |


| 593 | -0.9758 | 235.3906 | 3.8254 | 0.0015 |  | 101-10-M |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Polar | 235.2323 | -193.8527 | 94.0999 |  |  |  |
| 603 | -22.5818 | 233.1317 | 21.7699 | 0.0006 |  | 101-10-UL |
| Polar | 235.2493 | 195.3670 | 94.0575 |  |  |  |
| 613 | 17.0307 | 233.6052 | 21.9273 | 0.0006 |  | 101-10-UR |
| Polar | 235.2453 | 166.3163 | 105.9500 |  |  |  |
| 623 | 118.2240 | 202.1916 | -21.9545 | 0.0014 |  | 101-07-LL |
| Polar | 235.0637 | 154.3030 | 105.9409 |  |  |  |
| 63 3 | 153.9368 | 176.2914 | -21.9043 | 0.0009 |  | 101-07-LR |
| Polar | 235.3173 | 160.2564 | 98.6434 |  |  |  |
| 643 | 137.5171 | 190.8877 | 5.0140 | 0.0010 |  | 101-07-M |
| Polar | 235.2351 | 166.2536 | 93.9888 |  |  |  |
| 65 3 | 118.4071 | 202.0480 | 22.1787 | 0.0007 |  | 101-07-UL |
| Polar | 235.0814 | 154.2653 | 94.0258 |  |  |  |
| 66 3 | 154.0450 | 176.2048 | 22.0283 | 0.0009 |  | 101-07-UR |
| Polar | 234.7311 | 126.3335 | 106.2736 |  |  |  |
| 67 3 | 213.8915 | 93.8923 | -23.0942 | 0.0014 |  | 101-06-LL |
| Polar | 234.6309 | 114.1441 | 106.1531 |  |  |  |
| 68 3 | 227.7956 | 51.4600 | -22.6424 | 0.0013 |  | 101-06-LR |
| Polar | 234.7047 | 120.0094 | 99.1246 |  |  |  |
| 693 | 223.1856 | 72.5537 | 3.2273 | 0.0006 |  | 101-06-M |
| Polar | 234.7157 | 126.2829 | 93.9163 |  |  |  |
| 70 3 | 214.0140 | 93.7436 | 22.3961 | 0.0020 |  | 101-06-UL |
| Polar | 234.6782 | 113.9852 | 93.7104 |  |  |  |
| 713 | 227.9214 | 50.8908 | 23.1478 | 0.0016 |  | 101-06-UR |
| Polar | 236.1436 | 88.8155 | 123.1473 |  |  |  |
| 723 | 217.3080 | -38.5758 | -83.9818 | 0.0012 | 0.00 | 103-12-BM |
| Polar | 236.6288 | 58.6639 | 111.5386 |  |  |  |
| 73 3 | 185.3885 | -140.7300 | -42.6539 | 0.0008 |  | 103-04-TM |
| Polar | 236.5340 | 29.3336 | 117.1576 |  |  |  |


| $74 \quad 3$ | 101.3757 | -204.2177 | -62.9796 | 0.0022 |  | 103-08-M |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Polar | 236.5676 | -4.4287 | 123.1385 |  |  |  |
| 75 3 | -15.3696 | -220.5785 | -84.1021 | 0.0012 |  | 103-02-BM |
| Polar | 236.3402 | -34.7559 | 112.0152 |  |  |  |
| 763 | -120.5348 | -198.3984 | -44.3412 | 0.0008 |  | 103-05-TM |
| Polar | 236.2922 | -64.1656 | 122.8036 |  |  |  |
| 77 3 | -187.1532 | -118.0893 | -82.8409 | 0.0016 | 99.09 | 103-10-BM |
| Polar | 236.2426 | -96.1456 | 111.5393 |  |  |  |
| 78 3 | -231.9466 | -14.0602 | -42.5869 | 0.0026 |  | 103-13A-TM |
| Polar | 236.2621 | -126.4453 | 123.3518 |  |  |  |
| 793 | -201.7887 | 89.0025 | -84.7328 | 0.0026 |  | 103-11-BM |
| Polar | 236.3041 | -153.2887 | 111.1422 |  |  |  |
| 80 3 | -155.8239 | 172.8161 | -41.1475 | 0.0016 |  | 103-07-TM |
| Polar | 236.5436 | -187.1078 | 122.7141 |  |  |  |
| 813 | -44.5796 | 217.1171 | -82.6176 | 0.0013 |  | 103-01-BM |
| Polar | 236.5760 | 180.9556 | 111.8271 |  |  |  |
| 823 | 68.5209 | 222.1790 | -43.6985 | 0.0015 |  | 103-09-TM |
| Polar | 236.3447 | 149.0145 | 123.1349 |  |  |  |
| 83 3 | 158.6060 | 153.7700 | -84.0103 | 0.0010 |  | 103-03-BM |
| Polar | 236.0177 | 121.2223 | 112.1187 |  |  |  |
| 843 | 218.9959 | 75.8344 | -44.6575 | 0.0010 |  | 103-06-TM |
| Polar | 236.0282 | 101.5456 | 126.1856 |  |  |  |
| 85 3 | 216.2780 | 5.2517 | -94.3692 | 0.0015 |  | 103-12-BL |
| Polar | 236.3620 | 74.3597 | 126.1563 |  |  |  |
| 86 3 | 199.3523 | -84.9335 | -94.4031 | 0.0013 |  | 103-12-BR |
| Polar | 236.4406 | 70.7671 | 126.1395 |  |  |  |
| 87 3 | 194.3316 | -96.0850 | -94.3771 | 0.0014 |  | 103-04-BL |
| Polar | 236.6675 | 43.4039 | 126.0864 |  |  |  |
| 88 3 | 136.7967 | -168.5473 | -94.2868 | 0.0011 |  | 103-04-BR |
| Polar | 236.7008 | 39.7101 | 126.0808 |  |  |  |


| 893 | 126.8152 | -176.2281 | -94.2807 | 0.0006 |  | 103-08-BL |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Polar | 236.5956 | 12.6453 | 126.0711 |  |  |  |
| 903 | 42.8266 | -212.7642 | -94.2058 | 0.0015 |  | 103-08-BR |
| Polar | 236.5585 | 8.9059 | 126.0750 |  |  |  |
| 913 | 30.2568 | -214.8721 | -94.2044 | 0.0013 | 65.36 | 103-02-BL |
| Polar | 236.3872 | -18.0718 | 126.1052 |  |  |  |
| 923 | -60.7174 | -208.1137 | -94.2391 | 0.0013 |  | 103-02-BR |
| Polar | 236.3978 | -21.3828 | 126.1031 |  |  |  |
| 93 3 | -71.4581 | -204.6880 | -94.2362 | 0.0014 |  | 103-05-BL |
| Polar | 236.3208 | -48.1729 | 126.1429 |  |  |  |
| 943 | -148.7514 | -157.5447 | -94.3408 | 0.0010 |  | 103-05-BR |
| Polar | 236.3500 | -52.8331 | 126.1364 |  |  |  |
| 953 | -159.9022 | -146.2680 | -94.3306 | 0.0005 |  | 103-10-BL |
| Polar | 236.3504 | -79.0777 | 126.1733 |  |  |  |
| 963 | -205.0599 | -69.9282 | -94.4563 | 0.0010 |  | 103-10-BR |
| Polar | 236.3370 | -83.5278 | 126.1583 |  |  |  |
| 97 3 | -209.4529 | -55.4374 | -94.3998 | 0.0020 |  | 103-13A-BL |
| Polar | 236.2500 | -110.5427 | 126.1525 |  |  |  |
| 983 | -213.6310 | 35.7051 | -94.3451 | 0.0021 | 0.00 | 103-13A-BR |
| Polar | 236.2248 | -114.4475 | 126.1528 |  |  |  |
| 993 | -211.0176 | 48.7278 | -94.3364 | 0.0023 | 0.00 | 103-11-BL |
| Polar | 236.2857 | -140.7745 | 126.1259 |  |  |  |
| 1003 | -173.7243 | 129.4763 | -94.2692 | 0.0022 |  | 103-11-BR |
| Polar | 236.3106 | -145.0842 | 126.1275 |  |  |  |
| 1013 | -164.5837 | 140.9446 | -94.2844 | 0.0020 |  | 103-07-BL |
| Polar | 236.5107 | -171.9030 | 126.0890 |  |  |  |
| 1023 | -92.6622 | 196.1407 | -94.2330 | 0.0028 | 96.72 | 103-07-BR |
| Polar | 236.4963 | -176.0371 | 126.0813 |  |  |  |
| 1033 | -79.7380 | 201.7388 | -94.2010 | 0.0015 | 96.78 | 103-01-BL |
| Polar | 236.6531 | 197.5640 | 126.0600 |  |  |  |


| 1043 | 8.3052 | 216.9419 | -94.1910 | 0.0015 | 103-01-BR |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Polar | 236.6555 | 194.0186 | 126.0621 |  |  |
| 1053 | 20.3676 | 216.1425 | -94.1989 | 0.0011 | 103-09-BL |
| Polar | 236.6755 | 167.6112 | 126.0770 |  |  |
| 1063 | 105.7467 | 189.6006 | -94.2579 | 0.0009 | 103-09-BR |
| Polar | 236.5873 | 161.9710 | 126.0832 |  |  |
| 1073 | 122.0572 | 179.4260 | -94.2439 | 0.0009 | 103-03-BL |
| Polar | 236.1211 | 135.6967 | 126.1627 |  |  |
| 1083 | 183.3144 | 115.1136 | -94.3285 | 0.0021 | 103-03-BR |
| Polar | 236.0673 | 132.3806 | 126.1778 |  |  |
| 1093 | 188.9966 | 105.3781 | -94.3585 | 0.0011 | 103-06-BL |
| Polar | 236.0459 | 104.9025 | 126.1992 |  |  |
| 1103 | 215.6967 | 16.6435 | -94.4224 | 0.0015 | 103-06-BR |

## 6 Appendix B

## Measure

## EvENT SUMMARY

```
Job Name: 970706 103/105
Date: 98/02/15
Operator: robk
Job Comments:
Survey of the 103/105 panels taken on Jul 6, 1997.
The sphere center was got by fitting a circle to the bottom of the
105 panels, and translating upwards the nominal distance from the
circle center.
JOB SUMMARY
```

VALUES SHOWN IN: R Hand Inch Grads

| Event CS | \|-------- | COORDINATES | - | POINTING | APEX | I----EVENT |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. No. | X | Y | Z | ERROR | ANGLE | NAME |
| Polar | 236.1144 | 88.8163 | 123.1438 |  |  |  |
| 103 | 217.2862 | -38.5689 | -83.9593 | 0.0012 |  | 103-12-BM |
| Polar | 236.5788 | 58.6579 | 111.5418 |  |  |  |
| 113 | 185.3341 | -140.7167 | -42.6568 | 0.0008 |  | 103-04=TM |
| Polar | 236.4144 | 29.3140 | 117.1654 |  |  |  |
| 123 | 101.2582 | -204.1387 | -62.9756 | 0.0015 |  | 103-08-M |
| Polar | 236.3956 | -34.7839 | 112.0055 |  |  |  |
| 13 3 | -120.6537 | -198.3977 | -44.3160 | 0.0012 |  | 103-05-TM |
| Polar | 236.2659 | -64.1909 | 122.8016 |  |  |  |
| 143 | -187.1814 | -118.0031 | -82.8249 | 0.0000 | 51.46 | 103-10-BM |
| Polar | 236.2557 | -96.1802 | 111.5375 |  |  |  |
| 15 3 | -231.9683 | -13.9351 | -42.5827 | 0.0015 |  | 103-13-TM |
| Polar | 236.2805 | -126.4787 | 123.3475 |  |  |  |
| 163 | -201.7629 | 89.1178 | -84.7243 | 0.0021 |  | 103-11-BM |
| Polar | 236.4167 | -153.3141 | 111.1385 |  |  |  |


| 17 3 | -155.8308 | 172.9625 | -41.1535 | 0.0019 | 21.97 | 103-07-TM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Polar | 236.6081 | -187.1185 | 122.7091 |  |  |  |
| 18 3 | -44.5564 | 217.1902 | -82.6229 | 0.0003 | 30.16 | 103-01-BM |
| Polar | 236.6328 | 180.9471 | 111.8241 |  |  |  |
| 193 | 68.5675 | 222.2252 | -43.6982 | 0.0004 |  | 103-09-TM |
| Polar | 236.3660 | 149.0034 | 123.1302 |  |  |  |
| 203 | 158.6516 | 153.7605 | -84.0015 | 0.0008 |  | 103-03-BM |
| Polar | 236.0752 | 121.2195 | 112.1109 |  |  |  |
| 213 | 219.0577 | 75.8451 | -44.6401 | 0.0009 |  | 103-06-TM |
| Polar | 236.1764 | 100.6175 | 137.2631 |  |  |  |
| 223 | 196.8512 | 1.9094 | -130.4809 | 0.0021 | 49.37 | 105-02-M |
| Polar | 236.3133 | 69.9412 | 134.1376 |  |  |  |
| 23 3 | 180.9178 | -92.3927 | -120.7325 | 0.0006 |  | 105-05-M |
| Polar | 236.4545 | 38.1894 | 136.7591 |  |  |  |
| 243 | 111.8471 | -163.5294 | -129.0701 | 0.0016 |  | 105-09-M |
| Polar | 236.5214 | 7.6308 | 138.8722 |  |  |  |
| 253 | 23.1721 | -192.3921 | -135.6124 | 0.0006 |  | 105-04-M |
| Polar | 236.4965 | -22.7430 | 135.0908 |  |  |  |
| 263 | -70.4532 | -188.7499 | -123.8564 | 0.0002 |  | 105-07-M |
| Polar | 236.2800 | -53.9495 | 138.2490 |  |  |  |
| 27 3 | -146.0955 | -129.0068 | -133.5723 | 0.0015 | 50.14 | 105-12-M |
| Polar | 236.1749 | -85.2501 | 134.6260 |  |  |  |
| 283 | -196.6937 | -46.4054 | -122.2157 | 0.0007 |  | 105-01-M |
| Polar | 236.2160 | -114.8096 | 137.2308 |  |  |  |
| 293 | -191.6542 | 45.4062 | -130.4030 | 0.0019 |  | 105-08-M |
| Polar | 236.3051 | -146.0476 | 134.2182 |  |  |  |
| 303 | -152.1603 | 134.3499 | -120.9854 | 0.0008 |  | 105-10-M |
| Polar | 236.6528 | -179.3432 | 137.3464 |  |  |  |
| 313 | -62.8335 | 186.8019 | -131.0020 | 0.0010 | 32.50 | 105-06-M |
| Polar | 236.5120 | 191.8277 | 133.9805 |  |  |  |


| 323 | 26.0662 | 201.9373 | -120.3320 | 0.0007 |  | 105-03-M |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Polar | 236.4627 | 162.2421 | 136.2643 |  |  |  |
| 33 3 | 111.2973 | 165.1162 | -127.5309 | 0.0013 |  | 105-13-M |
| Polar | 236.0503 | 131.2854 | 135.2483 |  |  |  |
| 343 | 177.0225 | 94.7470 | -124.1200 | 0.0016 |  | 105-11-M |
| Polar | 236.2127 | 98.0670 | 143.4195 |  |  |  |
| 353 | 183.2858 | -5.5669 | -148.9019 | 0.0016 | 49.87 | 105-02-LM |
| Polar | 236.4383 | 67.1622 | 143.3695 |  |  |  |
| 363 | 159.7664 | -90.5903 | -148.8999 | 0.0009 |  | 105-05-LM |
| Polar | 236.5787 | 36.7302 | 143.3253 |  |  |  |
| 37 3 | 100.2994 | -154.1105 | -148.8605 | 0.0019 |  | 105-09-LM |
| Polar | 236.6290 | 9.8508 | 143.3144 |  |  |  |
| 383 | 28.3485 | -181.7420 | -148.8607 | 0.0009 |  | 105-04-LM |
| Polar | 236.4884 | -23.7683 | 143.3309 |  |  |  |
| 393 | -67.0359 | -171.1302 | -148.8201 | 0.0015 |  | 105-07-LM |
| Polar | 236.3696 | -52.0661 | 143.3773 |  |  |  |
| 403 | -133.9624 | -125.5377 | -148.8790 | 0.0002 | 49.28 | 105-12-LM |
| Polar | 236.2677 | -85.7790 | 143.4119 |  |  |  |
| 413 | -178.8733 | -40.6355 | -148.9144 | 0.0008 | 37.56 | 105-01-LM |
| Polar | 236.2992 | -115.5967 | 143.4003 |  |  |  |
| 423 | -178.0034 | 44.5034 | -148.9011 | 0.0004 | 3.58 | 105-08-LM |
| Polar | 236.4353 | -145.7185 | 143.3624 |  |  |  |
| 43 3 | -138.3138 | 120.8574 | -148.8774 | 0.0012 |  | 105-10-LM |
| Polar | 236.5560 | -176.2543 | 143.3090 |  |  |  |
| 443 | -67.0130 | 171.2508 | -148.7991 | 0.0024 | 34.05 | 105-06-LM |
| Polar | 236.6348 | 190.6378 | 143.2909 |  |  |  |
| 453 | 26.9617 | 182.0130 | -148.7965 | 0.0018 |  | 105-03-LM |
| Polar | 236.4720 | 160.2105 | 143.3303 |  |  |  |
| 463 | 107.5312 | 149.0377 | -148.8080 | 0.0008 | 39.08 | 105-13-LM |
| Polar | 236.1404 | 130.0174 | 143.4123 |  |  |  |

## 7 Appendix C

Measure<br>EVENT SUMMARY

Job Name: 970817 107-1C
Date: 98/02/15
Operator: robk
Job Comments:
Survey of the 105/107 panels taken on Aug 17, 1997.
The results are presented in the sphere center coordinate frame.
The sphere center was got by fitting a circle to the bottom of the 107 panels, and translating upwards the nominal distance from the circle center.

JOB SUMMARY
VALUES SHOWN IN: R Hand Inch Grads


| Polar |  | 236.2393 | -114.7789 | 137.2331 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15 | 3 | -191.6905 | 45.3172 | -130.4229 | 0.0049 |  | 105-08-M |
| Polar |  | 236.2810 | -146.0114 | 134.2218 |  |  |  |
| 16 | 3 | -152.2161 | 134.2448 | -120.9846 | 0.0004 |  | 105-10-M |
| Polar |  | 236.4976 | -179.3097 | 137.3700 |  |  |  |
| 17 | 3 | -62.8751 | 186.6004 | -130.9891 | 0.0001 | 61.08 | 105-06-M |
| Polar |  | 236.3363 | 191.8377 | 134.0045 |  |  |  |
| 18 | 3 | 26.0093 | 201.7464 | -120.3194 | 0.0011 |  | 105-03-M |
| Polar |  | 236.3217 | 162.2273 | 136.2762 |  |  |  |
| 19 | 3 | 111.2559 | 164.9723 | -127.4920 | 0.0021 |  | 105-13-M |
| Polar |  | 236.0940 | 131.2720 | 135.2378 |  |  |  |
| 20 | 3 | 177.0933 | 94.7370 | -124.1097 | 0.0016 |  | 105-11-M |
| Polar |  | 236.1738 | 103.9083 | 157.1311 |  |  |  |
| 21 | 3 | 147.0086 | 9.0365 | -184.6208 | 0.0012 | 64.01 | 107-04-M |
| Polar |  | 236.3036 | 66.3061 | 150.4911 |  |  |  |
| 22 | 3 | 143.1134 | -83.7109 | -168.3759 | 0.0010 |  | 107-06-M |
| Polar |  | 236.3020 | -5.4153 | 151.8416 |  |  |  |
| 23 | 3 | -13.7797 | -161.6016 | -171.8537 | 0.0014 |  | 107-05-M |
| Polar |  | 236.4866 | 31.4125 | 157.0163 |  |  |  |
| 24 | 3 | 70.0117 | -130.1821 | -184.5992 | 0.0008 | 62.04 | 107-01-M |
| Polar |  | 236.3177 | -45.1571 | 156.9019 |  |  |  |
| 25 | 3 | -96.4216 | -112.3329 | -184.2017 | 0.0014 |  | 107-03-M |
| Polar |  | 236.2660 | -83.8100 | 153.8526 |  |  |  |
| 26 | 3 | -151.6170 | -39.4113 | -176.8634 | 0.0021 |  | 107-02-M |
| Polar |  | 236.2995 | -122.8970 | 151.7525 |  |  |  |
| 27 | 3 | -152.0336 | 57.1679 | -171.6247 | 0.0007 |  | 107-10-M |
| Polar |  | 236.4452 | -153.6032 | 157.2765 |  |  |  |
| 28 | 3 | -97.9202 | 109.6827 | -185.1693 | 0.0007 |  | 107-09-M |
| Polar |  | 236.4003 | -197.4132 | 149.9591 |  |  |  |
| 29 | 3 | -6.7947 | 167.1296 | -167.0527 | 0.0021 | 61.65 | 107-07-M |


| Polar |  | 236.3424 | 178.2761 | 156.5007 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | 3 | 49.9350 | 140.6101 | -183.2841 | 0.0013 |  | 107-08-M |
| Polar |  | 236.1581 | 142.3027 | 151.6207 |  |  |  |
| 31 | 3 | 128.0702 | 100.3203 | -171.1857 | 0.0033 | 18.59 | 107-11-M |
| Polar |  | 236.2257 | 114.7281 | 160.1605 |  |  |  |
| 32 | 3 | 134.6812 | 31.7263 | -191.4601 | 0.0028 | 57.51 | 107-04-LL |
| Polar |  | 236.3128 | 88.5526 | 160.1559 |  |  |  |
| 33 | 3 | 136.2007 | -24.7584 | -191.5206 | 0.0014 |  | 107-04-LR |
| Polar |  | 236.3873 | 78.4341 | 160.1320 |  |  |  |
| 34 | 3 | 130.6742 | -46.0415 | -191.5291 | 0.0019 |  | 107-06-LL |
| Polar |  | 236.4965 | 52.1692 | 160.1094 |  |  |  |
| 35 | 3 | 101.3454 | -94.6641 | -191.5682 | 0.0027 |  | 107-06-LR |
| Polar |  | 236.4919 | 4.1655 | 160.0827 |  |  |  |
| 36 | 3 | 9.0726 | -138.4610 | -191.5063 | 0.0019 |  | 107-05-LL |
| Polar |  | 236.4486 | -20.9300 | 160.0879 |  |  |  |
| 37 | 3 | -44.7885 | -131.2873 | -191.4826 | 0.0010 |  | 107-05-LR |
| Polar |  | 236.5610 | 43.1438 | 160.0887 |  |  |  |
| 38 | 3 | 87.0157 | -108.1120 | -191.5755 | 0.0023 |  | 107-01-LL |
| Polar |  | 236.5449 | 16.6109 | 160.0913 |  |  |  |
| 39 | 3 | 35.7972 | -134.0662 | -191.5680 | 0.0005 | 62.73 | 107-01-LR |
| Polar |  | 236.4360 | -31.3291 | 160.0971 |  |  |  |
| 40 | 3 | -65.5260 | -122.2249 | -191.4926 | 0.0017 |  | 107-03-LL |
| Polar |  | 236.3778 | -60.2895 | 160.1290 |  |  |  |
| 41 | 3 | -112.4599 | -80.9281 | -191.5148 | 0.0039 | 49.32 | 107-03-LR |
| Polar |  | 236.3644 | -65.0066 | 160.1311 |  |  |  |
| 42 | 3 | -118.1301 | -72.3732 | -191.5085 | 0.0038 | 45.61 | 107-02-LL |
| Polar |  | 236.2890 | -97.3267 | 160.1455 |  |  |  |
| 43 | 3 | -138.3278 | -5.8122 | -191.4787 | 0.0037 |  | 107-02-LR |
| Polar |  | 236.2277 | -106.2055 | 160.1546 |  |  |  |
| 44 | 3 | -137.7297 | 13.4680 | -191.4489 | 0.0006 |  | 107-10-LL |


| Polar | 236.3547 | -132.7167 | 160.1275 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 453 | -120.6467 | 68.1059 | -191.4928 | 0.0009 |  | 107-10-LR |
| Polar | 236.4777 | -139.2297 | 160.1233 |  |  |  |
| 463 | -113.1296 | 80.1201 | -191.5833 | 0.0025 |  | 107-09-LL |
| Polar | 236.5048 | -166.9786 | 160.0914 |  |  |  |
| 47 3 | -68.7801 | 120.4900 | -191.5359 | 0.0008 | 64.43 | 107-09-LR |
| Polar | 236.4973 | -177.9348 | 160.0883 |  |  |  |
| 483 | -47.1317 | 130.4936 | -191.5229 | 0.0020 | 65.78 | 107-07-LL |
| Polar | 236.5588 | 195.9645 | 160.0757 |  |  |  |
| 493 | 8.7936 | 138.5393 | -191.5453 | 0.0000 | 66.20 | 107-07-LR |
| Polar | 236.5130 | 187.9075 | 160.0778 |  |  |  |
| 503 | 26.2038 | 136.2889 | -191.5127 | 0.0023 |  | 107-08-LL |
| Polar | 236.4394 | 160.1504 | 160.1018 |  |  |  |
| 513 | 81.2426 | 112.3782 | -191.5056 | 0.0021 |  | 107-08-LR |
| Polar | 236.4212 | 152.3846 | 160.1097 |  |  |  |
| 523 | 94.2900 | 101.6321 | -191.5079 | 0.0056 |  | 107-11-LL |
| Polar | 236.2175 | 123.1192 | 160.1477 |  |  |  |
| 53 3 | 129.3750 | 49.1637 | -191.4256 | 0.0018 |  | 107-11-LR |

